A Comparison of Genetic Algorithms using Super Mario Bros.

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Abstract

This project was designed to compare and contrast Evolving Behavior Trees (EBTs) with NeuroEvolution of Augmenting Topologies (NEAT), a Genetic Algorithm for the evolution of Artificial Neural Networks. We used *Super Mario Bros.* as a benchmark to compare these two techniques. The results showed that NEAT had a slightly higher maximum fitness while performing poorly in all other comparisons. EBTs performed strongly in rise time, evolution time, generalization, and complexity.
1 Introduction

Artificial intelligence (AI), while often portrayed negatively in movies, has impacted many aspects of today’s society. Ranging from video game AI such as *Left 4 Dead*\[2\] to facial recognition software \[9\], AI directly impacts how we view the world and what a computer is capable of accomplishing. Just as society looks for smarter technology as the demand and expectations rise, so too must the computers.

Ideally, society could have computers doing the majority of the routine tasks. However, AI is not mature enough where computers are able to be so integrated into everyday life. Looking at a smaller scale, we can do research into the learning ability and performance of various AIs.

There are multiple variations of Genetic Algorithms (GA) that can produce an effective AI, including Evolving Behavior Trees (EBT) and NeuroEvolution of Augmenting Topologies (NEAT). The question is: how do they compare?

Our research determines the relative strengths and weaknesses of these forms of AI. By doing so, we can gain a better understanding of when to apply one method over another. We used the platform of *Super Mario Bros.* to compare our AIs into quantitative data. This approach has been used before during competitions \[11\]. By comparing both methods on the same platform, we were able to obtain clear information regarding the strengths and weaknesses of both methods.
2 Background

2.1 Genetic Programming

The first paper published related to Genetic Programming (GP) was published in 1954 when Nils Aall Barricelli used evolutionary algorithms to try to simulate evolution [1]. Ten years later, in 1964, Lawrence J. Fogel applied this theory of GP to finite state machines. However, the first modern form of GP didn’t occur until 1985 when Michael L. Cramer applied these evolutionary algorithms to trees [4].

GAs are typically represented in binary strings; however, a variety of representations are available [13]. The evolutionary process starts with random individuals, known as chromosomes. The collection of individuals are known as a population. Each generation consists of a population of chromosomes. There are three operations to advance from one generation to another.

**Evaluation:** Each individual is evaluated using a fitness function at the start of each generation. This function assigns a numeric fitness to each individual, making it possible to compare individuals.

**Selection:** At the end of each iteration of the algorithm, the strongest individuals will both advance and go through crossover to create the next generation.

**Crossover:** Crossover, also known as breeding, is the action of swapping portions of information between two individuals in the population. For example, for a tree-based GA, the act of crossover would be taking a branch from one tree (one individual) and swapping it with another tree’s branch. This action creates two different child trees that are noticeably different from their parents. The goal of the crossover is to create
new individuals who are superior to their parents. However, crossover by itself is not sufficient to create significant changes from generation to generation.

**Mutation:** To add more variation to each generation, individuals should occasionally be mutated. This means randomly changing various bits of information of an individual. In the tree example, an individual could be mutated by taking one of its branches and replacing it with another random branch. After a mutation has occurred, it can then crossover with other individuals, diffusing the new information into the population.

Genetic Algorithms will typically run continuously, converging slowly to the optimal solution. However, by default, GAs do not terminate. In order to stop the program from infinitely looping, the GA must have a termination case. There are multiple ways of accomplishing this, including minimum solution, number of generations, computation time, and a plateau test. The minimum solution termination case makes the GA accept a solution if it meets the bare minimum requirements to complete the problem. A GA can also stop after a fixed number of generations. One could also let the GA run until a time or computation limit is reached. Lastly, the plateau test stops the GA after the fitness of each generation has stopped increasing.

There are many GP techniques available, such as extended compact genetic programming or probabilistic incremental program evolution. These techniques modify and extend the ideas of genetic programming to solve specific types of problems. However, the following experiments will focus on exploring both an evolving behavior tree and a neural network implementation of GAs.

### 2.2 Neural Networks

A neural network is an artificial intelligence technique inspired by how the brain works [12]. It consists of a set of neurons with weighted connections between them. Neurons can either be inputs, outputs, or hidden.
**Input:** Input neurons are given values based on input to the model being trained. In the case of *Super Mario Bros.*, this would be information such as Mario’s current power-up state, the locations of enemies, and the locations of blocks.

**Output:** Output neurons represent the output of the model. In the case of *Super Mario Bros.*, this would be button presses. For example, if the output neuron representing the run button had a value of 1, then the AI controller would press the run button.

**Hidden:** Hidden neurons are used to add more detail to the output of the neural network. If the original neural network’s output was represented by the function \( f(x) \), then adding a layer of hidden neurons would make the output \( g(f(x)) \), where \( g(x) \) is the hidden neuron’s activation function. Essentially, they act as if you fed the output of one neural network into the input neurons of another neural network. This allows for more complex functions to be modeled by the neural network, such as discontinuous functions.

![Neural Network Structure](image)

**Figure 2.1:** Neural Network Structure

### 2.2.1 Evaluation of Neurons

The output of each neuron is determined by its inputs and its activation function [3]. The input value for a neuron \((in_j)\) is determined by the value of each input \((x_i)\) and its
weight \( (w_i) \):

\[
\text{in}_j = \sum_i w_i \cdot x_i \tag{2.1}
\]

The output of a neuron is then computed using its activation function \( (g(x)) \):

\[
\text{out}_j = g(\text{in}_j) \tag{2.2}
\]

There are many possibilities for the activation function. The most basic function would be one that outputs 1 if \( \text{in}_j \geq 0 \) and 0 if \( \text{in}_j < 0 \). A more complex example would be a differentiable function, such as the sigmoid function:

\[
g(\text{in}_j) = \frac{1}{1 + e^{-\text{in}_j}} \quad p \in \mathbb{R} \tag{2.3}
\]

### 2.2.2 Learning

There are many ways to train the weights of a neural network. One of the most common methods is called backpropogation [12]. Backpropogation is a form of supervised learning where the neural network is trained based on a set of training data. The training data consists of the values for the input neurons and the expected values of the output neurons. At each step, the neural network is fed the training inputs and the actual output values are recorded. Then, the difference between the expected and actual output is used to update the weights of the neural network. This can be repeated as many times a necessary until the neural network is within the desired level of accuracy.

Supervised learning works well when it is feasible to create a large enough set of training data to train the neural network with. However, this can be difficult for a game like Super Mario Bros. where human error is almost impossible to avoid. Therefore, a more effective technique would utilize reinforcement learning to avoid introducing human error into the AI controller.
2.3 NeuroEvolution of Augmenting Topologies

One form of reinforcement learning that has proven extremely effective is NeuroEvolution of Augmenting Topologies (NEAT) [10]. NEAT combines genetic programming with neural networks to create a technique that is not only capable of finding the correct weights, but also the correct topology of a neural network.

2.3.1 Basic Structure

NEAT encodes neural networks using genes in a Genetic Program [10]. There are two types of genes: node genes and connection genes.

Node Genes: Node genes describe a neuron in the neural network. This includes input, output, and hidden neurons.

Connection Genes: Connection genes describe the connection between two node genes. A connection gene includes information about the in-node, out-node, connection weight, enable bit (whether or not the connection is currently being used), and an innovation number that helps to identify the origin on the connection gene [10].

2.3.2 Mutation

NEAT allows almost all parts of the neural network to mutate. As with every learning technique, NEAT allows the weight of a connection gene to change. However, NEAT also allows for topology changes through crossover and mutation. When adding a new node gene, an existing connection gene is split into two. One will have the old weight and the other will have a weight of 1. This ensures that the new node doesn’t change any calculations right away [10]. When adding a connection gene, the weight is randomly generated and it gets a new innovation number.
2.3.3 Innovation Numbers

As described in the previous section, connection genes have an innovation number that helps to identify when the gene was originally created [10]. Each time a new connection gene is added through a mutation, it is assigned a new innovation number. However, when a connection gene is added through mating, the innovation number stays the same. Therefore, there is an easy way to identify the source of the gene, which helps to prevent losing or duplicating connection genes during mating.

2.3.4 Crossover

Each generation, all of the NEAT neural networks are evaluated on the task for which they were designed. They are then assigned a fitness score based on how well they performed. The NEAT neural networks with the highest fitness scores are more likely to be selected for crossover. The NEAT crossover process is shown in Figure 2.2. First, innovation numbers are used to match the genes of the two parents [10]. Connection genes with the same innovation number originated from the same gene, so during crossover their weights are averaged to create a connection gene for the offspring. Next, the remaining genes are classified as either disjoint or excess. Disjoint genes have an innovation number within the range of the other parent’s innovation numbers. Excess genes have an innovation number outside of that range. Finally, the disjoint and excess genes of the parent with the highest fitness score are added to the offspring’s genome.
2.3.5 Speciation

When adding new genes to a genome, there is a chance that the fitness of the neural network will drop enough that it won’t survive until the next generation. In order to give each new gene a fair chance at proving itself, NEAT divides the population into species [10]. Species are created by grouping the population based on the compatibility distance $\delta$. This distance is a linear combination of the number of excess genes ($E$), the number of disjoint genes ($D$), and the average difference in weight of matching genes ($W$):

$$\delta = \frac{c_1 E}{N} + \frac{c_2 D}{N} + c_3 \cdot W$$  \hspace{1cm} (2.4)
as described by [10]. The weights $c_1$, $c_2$, and $c_3$ can be modified to change the weight of each of the three terms. $N$ is the size of the larger genome.

NEAT uses explicit fitness sharing to ensure that one species doesn’t become too big [10]. Therefore, the new fitness of an organism ($f'_i$) is determined by the equation:

$$f'_i = \frac{f_i}{N_s}$$

(2.5)

where $f_i$ is the original fitness and $N_s$ is the number of organisms in the species [10]. This has the effect of giving a higher fitness to smaller species and a lower fitness to heavily populated species. As stated by Kenneth Stanley, “The net desired effect of speciating the population is to protect topological innovation. The final goal of the system, then, is to perform the search for a solution as efficiently as possible.” [10] By protecting topological innovation, NEAT minimizes the amount of work required to find an efficient solution.

## 2.4 Evolving Behavior Trees

Behavior trees are a way to specify behavior for an artificial intelligence controller in a way that is easy to read and understand. They consist of conditional nodes and action nodes [8]. Behavior trees are traversed by starting at the root conditional node and following a specific path through the tree until an action node is reached. The action node that is reached is the final result of the tree.

**Conditional:** Conditional nodes are branching nodes in a tree that contain two child nodes. Each conditional node contains a conditional statement that can evaluate to either true or false. If the statement is true, then the first child node is evaluated. If the statement is false, the second child node is evaluated. For example, in Figure 2.3, the root conditional node is $\text{IfEnemyAtPosition}(0,1)$. If that condition is true, then the action node $\text{Right,Jump,Up}$ is evaluated. Otherwise, the conditional node $\text{IfMarioCanJump}$ is evaluated.
**Action:** Action nodes are the leaf nodes of a behavior tree. An action node specifies the final result of a behavior tree in the form of an action to perform. In games like *Super Mario Bros.*, these action nodes would contain a list of buttons to press. For example, in Figure 2.3, the action node `Right, Jump, Up` specifies that right, jump, and up buttons should be pressed.

A context-free grammar (CFG) can encode the behavior tree’s structure and behavior into a simple array of integers. These arrays can serve as chromosomes in a GA, allowing behavior trees to evolve. The combination of behavior trees with a GA is known as evolving behavior trees (EBTs).

![Example EBT](image.png)

**Figure 2.3:** Example EBT

### 2.4.1 Crossover

Once encoded with the CFG, two behavior trees can then be crossed over to create a child tree. This occurs by swapping sub-trees of the two parent trees. One can then evaluate...
the resulting behavior tree with a fitness test to ensure the breeding was successful.

2.4.2 Mutation

To mutate a behavior tree, a branch or node is replaced by a randomly generated branch or node. This change is independent of all other individuals in the generation. If the mutation improves the fitness of the tree, the changes will eventually diffuse into the rest of the population through crossover.

By designing a set of nodes to fit the restrictions of Super Mario Bros., we can evolve a behavior tree that is capable of navigating and completing many types of levels [8].

2.5 Super Mario Bros.

In Super Mario Bros., you play as a plumber named Mario as he attempts to reach the goal at the end of each level. You can make Mario move left and right, run, jump, and shoot fireballs. Mario must navigate various platforms and gaps while avoiding enemies to reach the goal. Enemies include Goombas, a small brown creature that resembles a mushroom, Koopas, a turtle-like creature, and piranha plants, enemies that extend from pipes before returning [7].

There are two items, called power-ups, that Mario can obtain to help him reach the goal. The first is a power mushroom that causes Mario to grow in size, allowing him to take an extra hit from an enemy before dying. The second power-up is the fire flower, which grants Mario the ability to launch fire balls at enemies, killing them on contact. The fire flower grants Mario the powers of the power mushroom as well [7].

There are various obstacles that Mario will face in each level. These range from basic obstacles, such as a gap that must be jumped over, to more complex obstacles, such as dead ends that require significant backtracking [6]. Hence, a successful player must possess the precise movements and timing to avoid these obstacles and complete the level [6].
The combination of complexity and simplicity in *Super Mario Bros.* makes it ideal for machine learning. The game is complicated enough that an AI controller that can not learn would not be able to complete the game. At the same time, *Super Mario Bros.* is simple due to the fact that the output can only be a combination of six button presses.

2.5.1 Mario AI Championship

In 2009, Sergey Karakovskiy and Julian Togelius unveiled a competition to create an artificial intelligence controller to play *Super Mario Bros.* [11]. The software was based on *Infinite Mario Bros*, a clone of *Super Mario Bros.*, created by Markus Persson. Modifications were made to the software to expose an API that facilitated the creation of artificial intelligence controllers. The goal of the competition was to serve as an ideal benchmark for various artificial intelligence methods [6].

2.5.2 Competition Results

Many different type of controllers were submitted, including those that utilized A* (a graph search algorithm), neural networks, genetic programming, and more. Each controller had to complete 40 different levels and their final score was the total distance traveled across all levels. In the end, the A* based controllers had a clear advantage over the competition with the best non-A* based controller doing only half as well as the weakest A* based controller [6], as seen in Figure 2.4.
2.5.3 Updated Competition

Based on the results of the 2009 competition, the 2010 competition included three different gameplay-based tracks: gameplay, learning, and Turing test. The gameplay track was identical in gameplay to the 2009 competition. The learning track was added so that learning-based controllers had a chance to be fully utilized. The controllers were given 10,000 iterations to play through a level before being scored. This allowed the learning-based artificial intelligence techniques to create a controller that specialized in one specific level instead of trying to perform well at all levels. Finally, the Turing test track was added to force controllers to behave as much like a human as possible. A group of non-expert humans scored each contestant on how much they thought the controller resembled a human player [6].

![Figure 2.4: 2009 Mario AI Competition Results](image)

<table>
<thead>
<tr>
<th>Competitor</th>
<th>approach</th>
<th>progress</th>
<th>levels</th>
<th>time left</th>
<th>kills</th>
<th>mode</th>
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</thead>
<tbody>
<tr>
<td>Robin Baumgarten</td>
<td>A*</td>
<td>46554.8</td>
<td>40</td>
<td>4878</td>
<td>331</td>
<td>76</td>
</tr>
<tr>
<td>Peter Lawford</td>
<td>A*</td>
<td>46554.8</td>
<td>40</td>
<td>4841</td>
<td>421</td>
<td>69</td>
</tr>
<tr>
<td>Andy Slusn</td>
<td>A*</td>
<td>47335.5</td>
<td>38</td>
<td>4822</td>
<td>294</td>
<td>67</td>
</tr>
<tr>
<td>Tend Ellingson</td>
<td>BR</td>
<td>40599.2</td>
<td>11</td>
<td>5510</td>
<td>201</td>
<td>22</td>
</tr>
<tr>
<td>Sergio Lopez</td>
<td>RB</td>
<td>18240.3</td>
<td>11</td>
<td>5119</td>
<td>83</td>
<td>17</td>
</tr>
<tr>
<td>Spencer Schramm</td>
<td>RH</td>
<td>17010.5</td>
<td>8</td>
<td>6403</td>
<td>94</td>
<td>24</td>
</tr>
<tr>
<td>Matthew Erickson</td>
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<td>12676.3</td>
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<td>6017</td>
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<td>37</td>
</tr>
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<td>6190</td>
<td>90</td>
<td>32</td>
</tr>
<tr>
<td>Sergio Pekarsky</td>
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<td>38</td>
</tr>
<tr>
<td>Matteo Perez</td>
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<td>4497</td>
<td>170</td>
<td>23</td>
</tr>
<tr>
<td>Alexander Puler</td>
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<td>43</td>
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<tr>
<td>Michael Talock</td>
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<td>3</td>
<td>5965</td>
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<tr>
<td>Glenn Hartmann</td>
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<td>out of memory</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table II: Results of the SGG Phase of the 2009 Mario AI Competition. Explanation of the acronyms in the "Approach" column: Rule-based, GP: Genetic Programming, NN: Neural Network, SM: State Machine, Lx: Layered Controller, GA: Genetic Algorithm. Explanation of column labels: Progress, as in the previous table; Levels: Number of Levels Cleared (Out to 40); Time Left: Sum of In-Game Seconds Left at the End of Each Level (a Higher Number Means that the Agent Finished the Level Faster); Kills: Number of Enemies Killed; Mode: Number of Mode Switches, Meaning the Number of Times the Agent Lost a Mode (Through Getting Hurt) or Gained a Mode (Through Collecting a Mushroom or Flower).
3 Methodology

We used the results of the Mario AI competitions as a benchmark to test EBTs and NEAT. This software was created by Sergey Karakovskiy and Julian Togelius for the 2012 Mario AI competition. It provided the interface to an instance of Super Mario Bros, which allowed us to obtain information about Mario’s current power-up state, the state of the current 21 × 21 tile screen, and the location of all on-screen enemies.

3.1 Mario Level Parameters

Mario started each level with the fire flower power-up, adhering to the level design used in the 2010 Mario AI competition [6]. This allowed our AI controller to use the fire flower ability to easily defeat enemies and take up to three hits before dying. Levels included the basic enemy types along with pits and various platforms. In addition, a small number of levels had increased difficulty by utilizing advanced enemy types, such as flying Goombas and Koopas, and larger pits to jump over.

3.1.1 Training Levels

We trained each AI on a total of 25 different levels. These levels consist of 20 difficulty 0 levels and five difficulty 1 levels. The difficulty 0 levels represented the level of challenge present in the actual Super Mario Bros. game. The difficulty 1 levels were significantly more difficult than the difficulty 0 levels and contained more enemies and more challenging terrain. Since there were 25 levels, the maximum possible fitness was 102,400.
3.1.2 Test Levels

To test the effectiveness of each type of AI controller, we tested the champion of generation 1000 on a series of levels that were not part of the training levels. This test judged how well the AI controllers could generalize to levels they hadn’t seen before. This also tested to see if the AI controller became overfit to the training levels.

3.2 AI Controller Parameters

3.2.1 Evolution Process

Each AI evolved in populations of 100 chromosomes. There were a total of 1000 generations for each evolution process. The chromosome with the highest fitness for each generation was saved as the champion of that generation.

3.2.2 Evaluating Fitness of Controllers

We evaluated the fitness of our artificial intelligence controllers by measuring the total distance traveled by Mario across the test levels. Each level was 4096 units long, so the maximum possible fitness for \( n \) levels was \( 4096 \cdot n \). This was the same metric used in the 2012 Mario AI competition [6]. If there were multiple controllers with the same fitness, the AI chose the controller with the smallest number of genomes.

3.2.3 Feature Sets

We tested three different feature sets. Each feature set provided the AI controller with information about Mario’s surroundings within a given radius, as seen in Figure 3.1. The three radii being tested were 1, 2, and 3, resulting in inputs of \( 3 \times 3 \), \( 5 \times 5 \), and \( 7 \times 7 \) blocks, respectively. For each block within the radius, the AI controller was given two pieces of information. The first indicated if there was a block in that position, and the
second indicated if there was an enemy in that position. Furthermore, each state space also included an additional two pieces of information to indicate if Mario was on the ground and if Mario can currently jump. The AI controllers learned to play Mario using only the limited information provided by these feature sets.

3.3 NEAT

Due to the complex nature of NEAT [10], we utilized an existing Java implementation. This implementation was called Another NEAT Java Implementation (ANJI) and was created by Derek James and Philip Tucker [5]. ANJI handled the complex details of NEAT, with content and behavior defined by a properties file that specified the values of each NEAT parameter.

The initial population of 100 chromosomes consisted of fully connected neural networks
with no hidden neurons. Each neural network started with 6 output neurons and between 20 and 100 input neurons based on the feature set. The weight of each connection was a random real number. At each generation, the fitness of each chromosome was calculated and a new generation was created based upon the specified NEAT parameters. These new chromosomes have updated connection weights and new hidden nodes that were likely to improve the fitness of the chromosomes.

We utilized the default settings provided by ANJI. These defaults included an add connection rate of 1%, an add neuron rate of 0.5%, a weight mutation rate of 80%, a survival rate of 20%, and a speciation threshold of 20%. The defaults provided by ANJI created an optimal environment for rapid evolution.

3.4 EBT

The AI controllers have six inputs to the running Mario game. These inputs correspond to the six controller buttons: left, right, up, down, jump, and run/fire. Thus, the output of the behavior trees was a combination of the six available buttons [7]. The behavior trees had to take a set of environmental and enemy conditions and select the appropriate action. Due to this requirement, the EBTs consisted of several types of conditional nodes and one type of action node.

**Conditional Nodes:** Conditional nodes create branches in the tree and were based on the terrain and enemy data point occurring around Mario. This also included if Mario has the ability to jump and if Mario is currently on the ground. Every block within Mario’s input radius was checked to see if there was a block or enemy present (Figure 3.1). The EBTs learned how to react in each situation. Each conditional node led to either another conditional node or the appropriate combination of buttons specified by an action node (Figure 2.3).

**Action Nodes:** Leaves in an EBT are known as action nodes. For Mario, these nodes
consist of a set of buttons to be pressed. The tree is then reevaluated after a single
frame passes in the Mario game.

We used a context free grammar to encode the EBT as a string of integers. These strings of
integers served as chromosomes in our GA, allowing our EBTs to evolve by swapping portions
of their encoding with portions of other EBTs’ encoding. At the end of each generation,
EBTs were selected for crossover based on their fitness. The higher the fitness, the more likely
they were to participate in crossover. The EBT with the highest fitness for that generation,
known as the “champion”, was carried over, unaltered, to the next generation. Over a large
number of iterations, this led to improvement of the AI controllers and eventually an EBT
that performed well at multiple levels.

Similar to NEAT, we implemented the genetic algorithm with a population size of 100.
We gave these individuals a maximum number of nodes to prevent unnecessary repetition.
The maximum number of nodes was based on the feature set: 200, 300, and 400 for $3 \times 3$, $5 \times 5$,
and $7 \times 7$ respectively. Unlike NEAT, we customized the EBT mutation and reproduction
probability to 30% and 10% respectively. Of those selected, the genetic algorithm chose 90%
for crossover and 10% for mutation. We also set the maximum initial depth, or how many
levels the initial trees can have, to eight. We chose these parameters based on a similar
example provided by the Java Genetic Algorithms Package.

We used Java Genetic Algorithms Package (JGAP http://jgap.sourceforge.net/) to define
our conditional and action nodes and run our genetic algorithm. This framework was entirely
written in Java. Overall, JGAP provided a solid foundation that allowed us to focus entirely
on writing our EBT grammar.

3.5 Comparisons

Both the NEAT and EBT algorithms were run with a population size of 100 for 1000
generations, once for each of the three feature sets. We compared them on a number of
aspects, including maximum fitness, learning speed, evolution timing, generalization, and complexity.

**Maximum Fitness:** The maximum fitness is the fitness of the champion AI from generation 1000.

**Rise Time:** For these experiments, our rise time was measured as the number of generations required to reach a fitness of 75%. This measured how quickly a particular algorithm could achieve an acceptable level of performance.

**Evolution Timing Data:** The timing data refers to the time necessary for each generation to evolve. That time is equal to the total time it takes to evaluate each chromosome on the training levels and perform crossover and mutation to generate a new population. Different algorithms completed generations at different rates.

**Complexity:** Complexity refers to the number of genes in a chromosome. In NEAT, the three types of genes are input nodes, hidden nodes, and output nodes. In EBTs, the two types of genes are conditional nodes and action nodes. A smaller model size is easier to evaluate and therefore more desirable.

**Generalization:** Generalization refers to how well an AI performs on levels that weren’t included in the training level set. This was measured by the average fitness across the test level set. AIs are more useful if they can complete levels that they haven’t seen before.
4 Data and Analysis

Over the course of each evolution process, we recorded important values for each generation, including the champion fitness, the champion complexity, and the time to complete the last generation. In addition, each champion was evaluated on a set of test levels to get a better insight into their strengths and weaknesses.

4.1 Training Data

During the training, we kept track of the maximum fitness so that we could compare the strongest AIs against each other.
4.1.1 NEAT

Figure 4.1, above, shows the maximum fitness of NEAT over the course of 1000 generations. The graph shows the maximum fitness of each generation for $3 \times 3$, $5 \times 5$, and $7 \times 7$ NEAT implementations in blue, green, and yellow, respectively.

The $3 \times 3$ was the strongest of the NEAT implementations. It learned the quickest as shown by generations one through 100. The $3 \times 3$ also had the highest performing champion after 1000 generations.

The $5 \times 5$ was almost as good as the $3 \times 3$ implementation. However, it learned slightly slower and peaked lower. The $5 \times 5$ also showed variable maximum fitness unlike most of the AIs. This is because NEAT is not guaranteed to keep the champion individuals from generation to generation.

The $7 \times 7$ was stopped at 457 generations due to its memory usage. It showed the worst
learning and maximum fitness. However, it was not far from $5 \times 5$ and $3 \times 3$ implementations. The computation requirements for the $7 \times 7$ were simply too high to judge its fitness after 457 generations.

### 4.1.2 EBT

![EBT Champion Fitness Over Time](image)

**Figure 4.2: EBT Training Data Results**

Figure 4.2, above, shows the results of EBT over the course of 1000 generations. The graph shows the maximum fitness of each generation for $3 \times 3$, $5 \times 5$, and $7 \times 7$ EBT implementations.

The $3 \times 3$ had the highest fitness of the EBT implementations. The $5 \times 5$ showed the worst learning and had the lowest final fitness. It showed an unique behavior in that it stayed below 20% fitness for the first 997 generations. Although this seems like an unlikely outcome, we attempted the $5 \times 5$ EBT implementation many times and ended up with similar results.
each time, suggesting that the $5 \times 5$ was unable to generalize as well as the $3 \times 3$ or learn as well as the $7 \times 7$.

The $7 \times 7$ had similar fitness to the $3 \times 3$ implementation. Both of them learned quickly and both peaked at about the same percentage. This is unusual as the radius in between them failed to learn as quickly or as well.

4.1.3 Comparisons

<table>
<thead>
<tr>
<th>Feature Set:</th>
<th>AI:</th>
<th>NEAT:</th>
<th>EBT:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$3 \times 3$</td>
<td>5 x 5</td>
<td>$3 \times 3$</td>
</tr>
<tr>
<td></td>
<td>7 x 7</td>
<td></td>
<td>5 x 5</td>
</tr>
<tr>
<td></td>
<td></td>
<td>7 x 7</td>
<td></td>
</tr>
<tr>
<td>Maximum Fitness:</td>
<td>86.9%</td>
<td>85.4%</td>
<td>81.9%</td>
</tr>
<tr>
<td></td>
<td>85.8%</td>
<td>75.3%</td>
<td>86.1%</td>
</tr>
</tbody>
</table>

Figure 4.3: Maximum Fitness Summary

The maximum fitness of EBTs and NEAT were similar. EBTs achieved a maximum fitness of 86.1% with the $3 \times 3$ feature set while NEAT achieved a maximum fitness of 86.9% with the $3 \times 3$ feature set. In contrast, the worst maximum fitness for EBTs was 75.3% from the $5 \times 5$ feature set while the worst maximum fitness for NEAT was 81.9% from the $7 \times 7$ feature set. Overall, the $3 \times 3$ NEAT produced the highest maximum fitness of 86.9%, beating out the $3 \times 3$ EBT by only 0.8%. Thus the difference in maximum fitness between the NEAT and EBT implementations was negligible.
4.2 Rise Time

The rise time varied significantly between the genetic algorithms and the feature sets. For the $3 \times 3$ feature set, both NEAT and EBT had a rise time of 17 generations. Due to the odd behavior of the $5 \times 5$ EBT, it had a rise time of 1000 generations while the $5 \times 5$ NEAT had a rise time of only 61 generations. For the $7 \times 7$ feature set, NEAT had a rise time of 128 generations while EBT had a rise time of only 15 generations.

In general, the EBT implementations had a faster learning rate than the corresponding NEAT implementations. Hence, EBTs are more effective for applications that require fast learning in a small number of generations.

### Rise Time:

<table>
<thead>
<tr>
<th>Feature Set:</th>
<th>AI: $3 \times 3$</th>
<th>NEAT: $5 \times 5$</th>
<th>7 x 7</th>
<th>EBT: $3 \times 3$</th>
<th>5 x 5</th>
<th>7 x 7</th>
</tr>
</thead>
<tbody>
<tr>
<td>25% Fitness:</td>
<td>8</td>
<td>16</td>
<td>21</td>
<td>16</td>
<td>998</td>
<td>10</td>
</tr>
<tr>
<td>50% Fitness:</td>
<td>9</td>
<td>28</td>
<td>38</td>
<td>16</td>
<td>998</td>
<td>10</td>
</tr>
<tr>
<td>75% Fitness:</td>
<td>17</td>
<td>62</td>
<td>128</td>
<td>18</td>
<td>998</td>
<td>15</td>
</tr>
</tbody>
</table>

Figure 4.4: Rise Time Summary
4.3 Evolution Timing Data

For the first 50 generations of each run, each generation took approximately three minutes to complete chromosome evaluation, crossover, and mutation. Since crossover and mutation were not computationally expensive, most of the three minutes was spent evaluating each chromosome on the training level set. However, as each run progressed beyond the first 100 generations, the time to evolve each generation grew. This is because the chromosomes grew larger over time, so by generation 100, their size started affecting the speed of evaluation, mutation, and crossover.

For the EBT runs, the time to evolve each generation grew linearly. The 3 × 3 run progressed from three minutes per generation at the start to about five minutes per generation at the end. The 5 × 5 run progressed from three minutes per generation to about seven minutes per generation, and the 7 × 7 run progressed from three minutes per generation to approximately eight minutes per generation. In total, the 3 × 3 run took about 21 hours to finish, the 5 × 5 run took 23.5 hours to finish, and the 7 × 7 run took 24.5 hours to finish.

The time to evolve each generation of the NEAT runs grew more rapidly than the EBT runs. This is due to the fact that fully connected neural networks are inherently more complex than behavior trees, and therefore require more time to process. While each of the runs began at three minutes per generation, the 3 × 3 run ended up taking over 15 minutes

\[
\begin{array}{|c|c|c|c|c|c|c|}
\hline
       & 3x3 NEAT & 5x5 NEAT & 7x7 NEAT & 3x3 EBT & 5x5 EBT & 7x7 EBT \\
\hline
Generation 1 & 2.5 & 3 & 3.5 & 2.5 & 3 & 3 \\
\hline
Generation 1000 & 15 & 25 & 90 & 5 & 7 & 8 \\
\hline
\end{array}
\]

Figure 4.5: Evolution Timing Data
per generation by generation 1000, resulting in a total computation time of over 30 hours. The $5 \times 5$ run progressed to taking about 25 minutes per generation by the end, resulting in a total time of 70 hours. By the time that the $7 \times 7$ run ran out of memory, the average generation took more than 90 minutes per generation to evolve, with a maximum of 122 minutes per generation. In total, the $7 \times 7$ implementation ran for over ten days before running out of memory at generation 457.

At the start of each evolution process, both EBT and NEAT took between three to five minutes to complete a generation. While all of the EBT implementations stayed under 15 minutes per generation throughout the whole process, the NEAT implementations took upwards of 120 minutes per generation by the end of the evolution process. Therefore, EBT is the more effective algorithm for applications that require quick results.
4.4 Complexity

4.4.1 NEAT

Figure 4.6: NEAT Champion Complexity Over Time

Figure 4.6, above, shows each the champion’s complexity for each generation of the NEAT evolution process. On average, the complexity increased over time for each input size while constantly fluctuating. This is indicative of the fact that NEAT divides each population into species that have different approaches to playing Mario. The champion complexity oscillates between two or three values, as small improvements are made by competing species, each with very different structures, but similar fitness.

In addition, the average complexity increased with input size. The maximum complexity of the $3 \times 3$ was 670, while the maximum complexity of the $5 \times 5$ was 4683. The $7 \times 7$ was significantly more complex, with a maximum complexity of 14803, despite the fact that it
only ran for 457 generations. If the trend continued linearly, the $7 \times 7$ would have reached a complexity of over 17000 by generation 1000.

### 4.4.2 EBT

![EBT Champion Complexity Over Time](image)

**Figure 4.7: EBT Champion Complexity Over Time**

Figure 4.7, above, shows the champion’s complexity for each generation of the EBT evolution process. EBTs often generated significant repetition throughout the evolution process. To help focus the evolution process, each input size was given a limit on the number of genes in its EBTs. These limits were chosen to reduce repetition while still allowing complex solutions to form. The $3 \times 3$ had a limit of 200 genes, the $5 \times 5$ had a limit of 300 genes, and the $7 \times 7$ had a limit of 400 genes.

During each evolution process, the average complexity quickly rose to the gene limit and fluctuated around that limit. This behavior was expected and often resulted in a series of
champions that had the same fitness but different complexity. For example, the champions of generation 820 and generation 998 for the $3 \times 3$ both had a fitness of 85.8%. However, the champion of generation 820, as seen in Figure 4.8, had a complexity of 49 while the champion of generation 998, as seen in Figure 4.9, had a complexity of 191.

Figure 4.8: $3 \times 3$ EBT from Generation 820

Figure 4.9: $3 \times 3$ EBT from Generation 998
4.4.3 Comparisons

Because the EBTs were limited to a set number of genes, the EBTs ended up with a much lower complexity than the corresponding NEAT implementations. However, even without the limit in place, the EBTs that were generated were less complex than the NEAT equivalents. This is because a fully connected neural network is inherently more complex than a behavior tree. Therefore, given two AIs of equal fitness, the EBT AI will likely be less complex than the NEAT AI.

4.5 Test Data

The final champion of each feature set was tested against a series of previously unseen levels to more accurately test its ability to generalize to new Mario levels. Due to the fact that the training levels consisted of difficulty 0 and difficulty 1 levels, the test levels consisted of 1000 difficulty 0 levels and 1000 difficulty 1 levels.
4.5.1 Difficulty 0 Test Levels

Figure 4.10 shows the average fitness of each champion for the 1000 difficulty 0 test levels. In addition, it also includes error bars to demonstrate the wide range of skill levels across different levels in the test level set.

In general, the $3 \times 3$ of each method performed better than the $5 \times 5$, which in turn performed better than the corresponding $7 \times 7$. We observed this in the training data as well, but the test level data highlights the true difference in fitness between each champion.

While Figure 4.10 shows the average fitness across all 1000 levels, that metric doesn’t necessarily show how many individual levels each champion fully completed. Therefore, Figure 4.11 shows the percentage of levels that each champion fully completed.
Figure 4.11 shows an even larger difference in levels completed between NEAT and EBTs. This highlights the fact that the larger input sizes were worse at generalizing to the easy levels. This is especially true for NEAT, where certain champions would just stop moving in the middle of a level. The EBT champions didn’t exhibit this phenomena due to the difference in how EBTs and NEAT generalize. NEAT neural networks start fully connected and connections are never removed. Hence, every output of the neural network is dependent on every input, so the neural network must be able to adapt to every permutation of inputs. However, behavior trees only utilize a subset of the possible inputs, and therefore only need to adapt to a smaller portion of the possible permutations of input.

Figure 4.11: NEAT vs. EBT Difficulty 0 Test Levels Completed

Overall, for difficulty 0 levels, the $3 \times 3$s outperformed the $5 \times 5$s, which in turn outperformed the $7 \times 7$s. Furthermore, the EBT champion for each input size outperformed the corresponding NEAT champion.
4.5.2 Difficulty 1 Test Levels

![NEAT vs. EBT Difficulty 1 Test Level Fitness](image)

Figure 4.12: NEAT vs. EBT Difficulty 1 Test Level Fitness

Figure 4.12, above, shows the average fitness of each champion over 1000 difficulty 1 test levels.

In general, the performance across difficulty 1 levels was significantly worse than the performance across difficulty 0 levels. For the EBT champions, the larger input sizes performed better than the smaller input sizes. While this trend doesn’t apply to the NEAT champions, it is possible that it would if the $7 \times 7$ run had a chance to make it past generation 457.

Out of all 1000 difficulty 1 levels, only one champion managed to complete a single level in its entirety. That champion was the $7 \times 7$ EBT and it managed to complete the level with seed 745. Based on this fact and the trends observed in Figure 4.12, it is evident that larger input sizes have an advantage in more difficult levels where larger groups of enemies and more difficult terrain is present.
4.6 Generalization

The ability for each champion AI controller to generalize was measured by their average fitness on the series of test levels and by their ability to perform competently on levels that they couldn’t complete.

For the difficulty 0 test levels, the EBT champions generalized better than the NEAT champions. The EBT champions achieved 2.2% to 5.7% higher fitness than their corresponding NEAT champions. In addition, there were locations in the test levels where the NEAT champions would get stuck and no longer proceed, despite the fact that those locations posed very little challenge. For example, Figure 4.13 shows where the $7 \times 7$ NEAT champion got stuck on the test level with seed 32. At 6% of the way through the level, the $7 \times 7$ NEAT champion decided to stay crouched on a block and remain that way until time ran out.

![Figure 4.13: 7 x 7 NEAT Champion Stuck on Level Seed 32](image)
For the difficulty 1 test levels, the clear winner was the $7 \times 7$ EBT. While the $3 \times 3$ and $5 \times 5$ NEAT champions outperformed the corresponding EBT champions, the $7 \times 7$ outperformed every other champion by at least 4.1%. In addition, the issue of getting stuck part way through the level wasn’t as big of an issue for the difficulty 1 levels as it was for the difficulty 0 levels. This was because most of the champions died well before they could get stuck. Overall, the smaller input sizes outperformed the larger input sizes on difficulty 0 levels, while the reverse was true on the difficulty 1 levels. The $3 \times 3$ feature set was great at generalizing to unseen easy levels, while the $7 \times 7$ feature set excelled at adapting to complex situations in the difficult levels.
5 Recommendations

5.1 When to use NEAT

NEAT’s biggest strength is maximum fitness. NEAT showed a slightly higher maximum fitness of 86.9% as opposed to EBTs maximum fitness of 86.1%. However, in most situations, an increase of 0.8% maximum fitness is not worth the huge increase in evolution and rise time. In addition, NEAT’s inability to generalize effectively negates its maximum fitness advantage. Therefore, NEAT should only be used when extreme amounts of computational power can be used to evolve NEAT with a large training set over thousands of generations to make effective use of its maximum fitness advantage.

5.2 When to use EBTs

EBTs were stronger than NEAT at all aspects of the evolution process except for maximum fitness. They generalized better, completed the evolution process faster, and had a higher learning speed. These strengths make EBTs better when time and processing power are limitations. EBT and NEAT also showed similar maximum fitness, only separated by .8%. Furthermore, EBTs are human readable, as shown in Figure 2.3, while neural networks are not. Due to all these strengths, EBTs are better for the majority of situations.
6 Areas for Future Work

6.1 New Features

This paper only covered the results of $3 \times 3$, $5 \times 5$, and $7 \times 7$ implementations. However, other feature sets could be constructed that may produce better results. Instead of using grid based features, one could implement a radial search for enemies or terrain. One could also group locations based on their distance from Mario. Locations close to Mario would be treated like they were in the $3 \times 3$ feature set, while further away locations may be grouped together to reduce the total number of features. This could help the AI prioritize the features of nearby locations while still being aware of far away terrain and enemies.

6.2 Improved Training Levels

Due to restrictions in computation power and time, we used a total of 25 training levels to train the AIs. However, by increasing the number and variety of training levels, one could produce an AI that not only generalizes better, but also can complete more difficult levels. There are a total of nine difficulty settings and three level themes that are available for use in the Mario level generation framework. The higher difficulty settings introduce new enemy types, such as spiky shell Koopas, that pose a greater challenge for the AI controller. In addition, the other level themes introduce new types of terrain challenges, such as locations that require backtracking to proceed.
6.3 Other AI Techniques

This paper covered NEAT and EBTs, but there are many other types of AIs capable of playing *Super Mario Bros*. There were a number of AIs used during the *Super Mario Bros.* competitions including: A*, Q-Learning, and syntax trees. One could compare any of these AIs along with NEAT and EBTs.
7 Conclusion

Both NEAT and EBTs were capable of producing an AI that could complete a variety of Super Mario Bros. levels. Each genetic algorithm excelled in certain comparison metrics while falling short in others. The results showed that NEAT had a slightly higher maximum fitness while performing poorly in all other comparisons. EBTs performed strongly in all other comparisons, including rise time, evolution time, generalization, and complexity. Due to how small the difference in maximum fitness between NEAT and EBTs was, we concluded that EBT is the stronger genetic algorithm for playing Super Mario Bros.
Glossary

AI  Artificial Intelligence

BT  Behavior Tree

CFG  Context-free Grammar

EA  Evolutionary Algorithm

EBT  Evolving Behavior Tree

EBTs  Evolving Behavior Trees

JGAP  Java Genetic Algorithms Package

GA  Genetic Algorithm

GP  Genetic Programming

NEAT  NeuroEvolution of Augmenting Topologies
Bibliography


